Individual Teaching/Learning Interviews to Facilitate Student Problem Solving

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AAPT Summer Meeting 2009
Ann Arbor, MI – July 27th 2009

This work is supported in part by NSF grant 0816207
Objective and Research Questions

Objective: Facilitate students’ transfer of problem solving skills across problems of different contexts and representations

Research Questions:

- What kinds of difficulties do students have when solving problems of different contexts and representations?
- How does the sequence in which problems of different contexts and representations are presented to students affect their performance?
- What kinds of scaffolding may help students overcome those difficulties?
Methodology
Teaching/Learning Interviews¹

- Calculus-based physics volunteers (N = 20)
- Each participant was interviewed 4 times during semester.
- Each interview came after an in-class exam.
- Each interview, the students were:
  - Asked to solve three problems:
    - Original problem: a problem from most recent exam
    - Graphical problem: part of info. given as graph
    - Functional problem: part of info. given as function
  - Asked to think aloud while solving problems.
  - Given verbal hints whenever unable to proceed.

¹Engelhardt, et. al. 2003
A spring of spring constant 3.0 kN/m is compressed a distance of 1.5 cm and a small ball is placed in front of it. The spring is then released and the small ball, mass 0.1 kg, is fired along the slope and launched into the air at point A which is 10 cm above the spring. The angle $\theta$ of velocity at launch is 30°. Friction is negligible.

What is the speed of the ball at the launch point (point A)?
Functional problem in Interview 2

A 0.1 kg bullet is loaded into a gun (muzzle length 0.5 m) compressing a spring to a maximum of 0.2 m as shown. The gun is then tilted at an angle of 30° and fired.

The only information you are given about the gun is that the barrel of the gun is frictionless and that the gun contains a non-linear spring such that when the held horizontal, the net force, F (N) exerted on a bullet by the spring as it leaves the fully compressed position varies as a function of the spring compression, x (m) as given by:

\[ F = 1000x + 3000x^2 \]

What is the muzzle velocity of the bullet as it leaves the gun, when the gun is fired at the 30° angle as shown above?
Examples of Interview Problems

Graphical problem in Interview 2

A 0.1 kg bullet is loaded into a gun (muzzle length 0.5 m) compressing a spring as shown. The gun is then tilted at an angle of 30° and fired.

The only information you are given about the gun is that the barrel of the gun is frictionless and when the gun is held horizontal, the net force $F$ (N) exerted on a bullet by the spring as it leaves the fully compressed position varies as a function of its position $x$ (m) in the barrel as shown in the graph below.

What is the muzzle velocity of the bullet as it leaves the gun, when the gun is fired at the 30° angle as shown above?
Results : Difficulties

- GRAPH: unable to process information from the graph provided.
- FUNCTION: inappropriate interpretation or use of the function given.
- PRINCIPLE: inappropriate use of physical principles.
- QUANTITY: incorrect use, calculations, and units of physical quantities.
- FORMULA: incorrectly recalls a formula or interpret meaning of formulae/expressions.
- VALUE: uses incorrect value of physical quantities.
- MATH: unable to manipulate mathematical processes.
- CALCULATION: simple calculation errors.
Results: Hints

- **GRAPH:** enables students to read off and process information from the graph provided.

- **QUANTITY:** helps students plan a strategy to find desired quantities using the info. given (e.g. graph, function), or to decide which quantities are applicable in each situation.

- **MATH:** questions on meaning of mathematical notations and operators.

- **PRINCIPLE:** enables students to determine the appropriate principle to use.

- **INFO:** asks students to take a more careful look at the problem statement to gather necessary data.

- **FORMULA:** helps students understand the meaning of a formula or an equation.

- **CALCULATION:** helps students recognize and correct simple calculation errors.
DIFFICULTIES: G-F SEQUENCE

# OF DIFFICULTIES PER STUDENT

PRINCIPLE

QUANTITY

FORMULA

VALUE

MATH

GRAPH

FUNCTION

CALC

ERROR

ORIGINAL

GRAPHICAL

FUNCTIONAL
DIFFICULTIES: F-G SEQUENCE

# OF DIFFICULTIES PER STUDENT

- PRINCIPLE
- QUANTITY
- FORMULA
- VALUE
- MATH
- GRAPH
- FUNCTION
- CALC
- ERROR

- ORIGINAL
- FUNCTIONAL
- GRAPHICAL
Results: Sequencing Effect

Representational aspect

- G-F sequence: most difficulties with graph
- F-G sequence: minor difficulty with function
- Students’ transfer occurs more easily in the F-G sequence than in the G-F sequence.
Results: Sequencing Effect

Contextual aspect (from Original to 2\textsuperscript{nd} problem)

- From Original to Graphical: minor difficulties with principle and quantities.

- From Original to Functional: some difficulties with principle and significant difficulties with quantities.
Conclusions

- Students were unable to interpret physical meaning of mathematical operators and processes.
  - Thus had difficulties solving problems in graphical and functional representations.

- When the context of the problem changed, could not relate the new problem to the original problem.
  - Thus had difficulties identifying the principle and physical quantities needed to solve the new problem.

- The sequence of problems affected their performance:
  - Representational Change: Easier when Functional problem is presented before Graphical problem.
  - Contextual Change: Harder when accompanied by representational change from Numerical to Graphical.
THANK YOU